

# FACULTY OF SCIENCE

#### **CLASS DESCRIPTOR**

# **DEPARTMENT OF MATHEMATICS & STATISTICS**

Class Code: MM307 Class Title: Stochastics and Financial

**Econometrics** 

Type: UG Level: 3 Credits: 20 Semester: 2

Class Coordinator: Dr J Pan Tel: 2853 Email: jiazhu.pan@strath.ac.uk

Teaching Staff: Dr J Pan/Professor X Mao

Pre-requisites: MM304 or equivalent.

Students: Compulsory: MS Optional: M, MT, MSA, MSE, MSMS, MSF

Overlaps:

### **CLASS DELIVERY (HOURS)**

LECTURES	TUTORIALS	LABORATORIES	ASSIGNMENTS	SELF STUDY	TOTAL
48	12	12	24	104	200

## **CLASS ASSESSMENT**

3 hour degree examination in May with August resit.

#### **GENERAL AIMS**

- To introduce the basic concepts of random phenomena evolving in time, from two complementary points of view: probabilistic modelling and data-driven analysis.
- To present underlying ideas of simple stochastic processes, time series models, and the associated probability theory and statistical techniques.
- To present applications of the methods to financial and economic systems, including modelling, data analysis, and forecasting.

#### **LEARNING OUTCOMES**

On completion of this class, the student should be able to

- understand and apply appropriate methods from probability theory;
- analyse simple stochastic models (Markov chains, Poisson and renewal processes, queueing systems);
- understand basic concepts of time series (stationarity, trend, seasonality, and autocorrelation);
- identify and interpret various time series models, and choose appropriate methods for analysing a given time series.
- apply methods of analysis and forecasting to financial and economic systems in the presence of volatility.

#### **SYLLABUS**

**Markov chains:** Markov models in finance, Markov property, n-step transition probabilities, classification of states, stationary distribution, 1<sup>st</sup>-step analysis, simple random walk.

**Poisson processes:** Poisson processes as insurance claim number processes, independent and stationary increments, inter-arrival and waiting time distributions, thinning, superposition.

**Renewal processes:** Risk models, renewal sequence, renewal process, arrival times, inter-arrival times, renewal function and equation, renewal theorem, some basic premium principles.

**Queueing theory:** Poisson arrivals, exponential service times, single or multiple servers, probability distribution of queue size, stationary distribution, M/M/1 queue, M/M/1 queue with baulking, M/M/∞ queue, M/M/s queue.

**Characteristics of financial time series:** Asset returns, time plots, review of statistical distributions, distributions of returns, likelihood function of returns, empirical properties of returns.

**Fundamental concepts:** Variance and covariance, correlation and autocorrelation function, stationarity, deterministic versus stochastic trends, seasonality, regression methods, residual analysis.

**Linear time series:** White noise, sample autocorrelation function, Box-Jenkins approach, autoregressive models (properties, partial autocorrelation, identification, estimation), moving average models (properties, identification, estimation), ARMA models, ARIMA models.

**Volatility models:** Characteristics of financial volatilities, conditional heteroscedasticity, structure of volatility model, ARCH models (properties, estimation and tests), application to analysis of financial data, value-at-risk.

**Forecasting:** Minimum mean-square error forecasting, forecasting using AR, MA and ARMA models, deterministic trends and ARIMA forecasting, forecasting evaluation.

## **RECOMMENDED TEXT/READING**

Ross, S.M. "Introduction to Probability Models" (Academic Press, 10<sup>th</sup> Ed.). ISBN: 0123756863.

Pinsky, M.A., & Karlin, S. "*An Introduction to Stochastic Models*" (4th edition, Academic Press, 2011). ISBN: 9780123814166.

Cryer, J.D. & Chan, K.S. "Time Series Analysis with Applications in R" (Springer, 2<sup>nd</sup> Ed.). ISBN: 9780387759586.

Tsay, R.S. "Analysis of Financial Time Series" (Wiley). ISBN: 9780471690740.

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