

## Formulas

### Significance Test and Confidence Interval for One Population

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i, \quad s^2 = \frac{1}{n-1} [\sum_{i=1}^n x_i^2 - n\bar{x}^2], \quad s = \sqrt{s^2}.$$

$$z\text{-test: } z = \frac{\bar{x} - \mu_0}{\sigma/\sqrt{n}},$$

$$(1 - \alpha)100\% \text{ C.I. for } \mu: \bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}},$$

$$t\text{-test: } t = \frac{\bar{x} - \mu_0}{s/\sqrt{n}},$$

$$(1 - \alpha)100\% \text{ C.I. for } \mu: \bar{x} \pm t_{\alpha/2, n-1} \frac{s}{\sqrt{n}}.$$

### Chi-Square Test

$$X^2 = \sum_{i=1}^k \frac{(n_i - np_i)^2}{np_i} \text{ which obeys a } \chi^2\text{-distribution with } k - 1 \text{ d.f.}$$

### Regression and Correlation

$$\bar{x} = \frac{1}{n} \sum_{i=1}^n x_i, \quad \bar{y} = \frac{1}{n} \sum_{i=1}^n y_i,$$

$$S_{xx} = \sum_{i=1}^n x_i^2 - n\bar{x}^2,$$

$$S_{xy} = \sum_{i=1}^n x_i y_i - n\bar{x}\bar{y},$$

$$S_{yy} = \sum_{i=1}^n y_i^2 - n\bar{y}^2,$$

$$\hat{a}_1 = \frac{S_{xy}}{S_{xx}}, \quad \hat{a}_0 = \bar{y} - \hat{a}_1 \bar{x}.$$

The least squares linear regression equation:  $\hat{y} = \hat{a}_0 + \hat{a}_1 x$ .

The correlation coefficient:  $r = \frac{S_{xy}}{\sqrt{S_{xx} S_{yy}}}$ .

The correlation is significantly different from zero at the  $\alpha$  level of significance if

$$|r| \sqrt{\frac{n-2}{1-r^2}} \geq t_{\alpha/2, n-2}.$$

### CRD

$$T_i = \sum_{j=1}^n x_{ij}, \quad \bar{x}_i = \frac{T_i}{n}, \quad T = \sum_{i=1}^c T_i,$$

$$SS_{total} = \sum_{i=1}^c \sum_{j=1}^n x_{ij}^2 - \frac{T^2}{cn},$$

$$SS_{treat} = \frac{1}{n} \sum_{i=1}^c T_i^2 - \frac{T^2}{cn},$$

$$SS_{error} = SS_{total} - SS_{treat},$$

$$MS_{treat} = \frac{SS_{treat}}{c-1}, \quad MS_{error} = \frac{SS_{error}}{c(n-1)},$$

$$F = \frac{MS_{treat}}{MS_{error}}.$$

$$s = \sqrt{MS_{error}}.$$

$$(1 - \alpha)100\% \text{ C.I. for } \mu_i: \bar{x}_i \pm t_{\alpha/2, c(n-1)} s \sqrt{\frac{1}{n}}.$$

$$(1 - \alpha)100\% \text{ C.I. } \mu_i - \mu_j: \bar{x}_i - \bar{x}_j \pm t_{\alpha/2, c(n-1)} s \sqrt{\frac{2}{n}}.$$

### RBD

$$B_i = \sum_{j=1}^c x_{ij}, \quad \bar{B}_i = \frac{B_i}{c}, \quad T_j = \sum_{i=1}^r x_{ij}, \quad \bar{x}_j = \frac{T_j}{r},$$

$$G = \sum_{i=1}^c T_i, \quad \bar{G} = \frac{G}{rc},$$

$$SS_{total} = \sum_{i=1}^r \sum_{j=1}^c x_{ij}^2 - \frac{G^2}{rc},$$

$$SS_{treat} = \frac{1}{r} \sum_{j=1}^c T_j^2 - \frac{G^2}{rc},$$

$$SS_{block} = \frac{1}{c} \sum_{i=1}^r B_i^2 - \frac{G^2}{rc},$$

$$SS_{error} = SS_{total} - SS_{treat} - SS_{block},$$

$$MS_{treat} = \frac{SS_{treat}}{c-1}, \quad MS_{block} = \frac{SS_{block}}{r-1}, \quad MS_{error} = \frac{SS_{error}}{(r-1)(c-1)}, \quad s = \sqrt{MS_{error}}.$$

$$F\text{-test for treatments: } F = \frac{MS_{treat}}{MS_{error}} > F_{\alpha, c-1, (r-1)(c-1)}.$$

$$F\text{-test for blocks: } F = \frac{MS_{block}}{MS_{error}} > F_{\alpha, r-1, (r-1)(c-1)}.$$

$$(1 - \alpha)100\% \text{ C.I. for } \mu_j: \bar{T}_j \pm t_{\alpha/2, (r-1)(c-1)} s \sqrt{\frac{1}{r}}.$$

$$(1 - \alpha)100\% \text{ C.I. for } \mu_j - \mu_k: \bar{T}_j - \bar{T}_k \pm t_{\alpha/2, (r-1)(c-1)} s \sqrt{\frac{2}{r}}.$$